

Problems -10/30/2025

The solutions to the problems below will be published on Sunday 11/02/2025

Problem 1. The functions f and g are defined on the set of real numbers and satisfy the system of equations

$$\begin{cases}
f(x) + 2g(1-x) = x^2 \\
f(1-x) - g(x) = x^2
\end{cases}$$
(1)

By what formula is f(x) expressed?

Problem 2. A regular hexagon is given. Tosia and Mateusz play a game consisting of drawing diagonals – alternately they draw diagonals joining two vertices, however the diagonals they draw are not allowed to intersect. The player who cannot make a move loses. Tosia starts the game; determine who will win the game and what the winning strategy is.

Good Luck!

We encourage you to submit your solutions via the website: https://mathlovers.eu/submit-solution/!